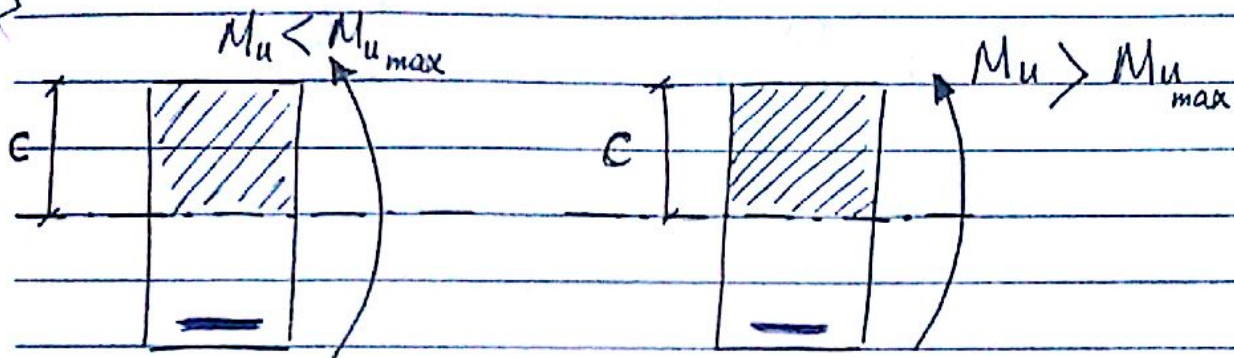


* Double Reinforcement (Rec. section)

Rec: $\frac{c}{d} > \frac{c_{max}}{d}$ Unsafe $\left\{ \begin{array}{l} \rightarrow \text{increase dim. (t)} \\ \rightarrow \text{Comp. steel} \end{array} \right.$



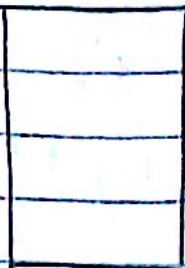
$$c < c_{max}$$

$$c > c_{max}$$

unsafe $\left\{ \begin{array}{l} \rightarrow \text{Make Bigger (t)} \\ \rightarrow \text{Double. R.} \end{array} \right.$

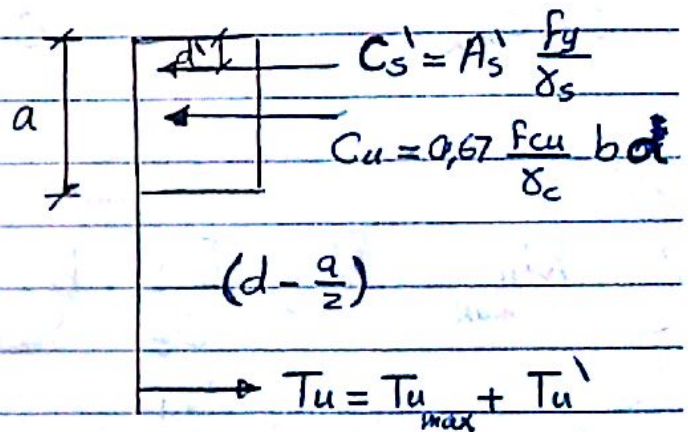
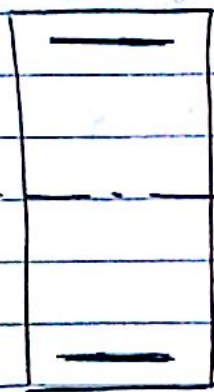
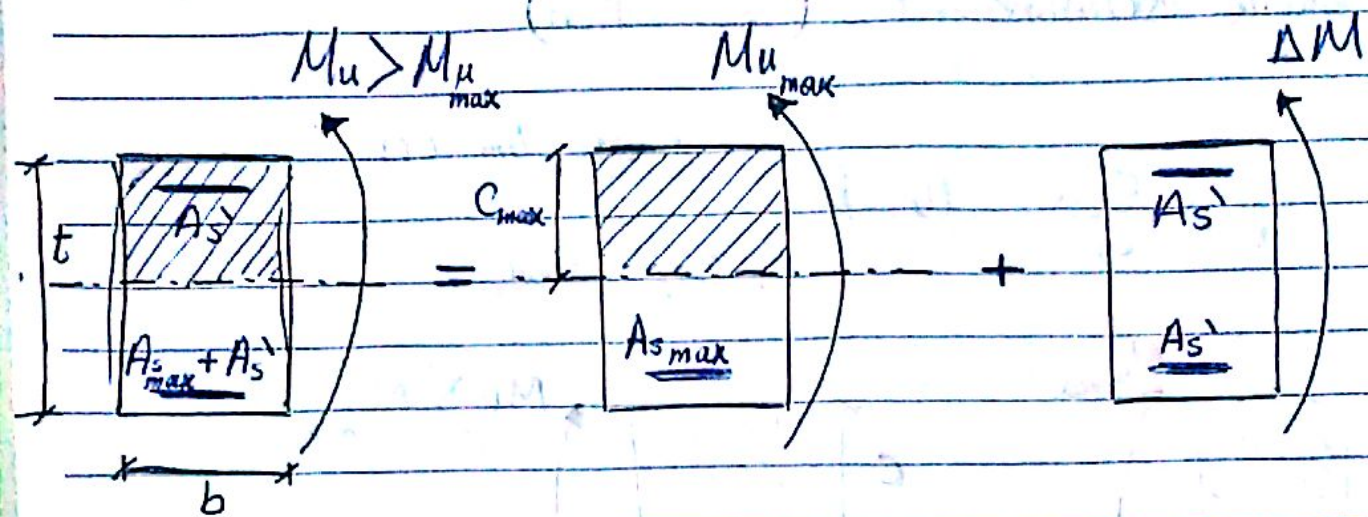
$$M_{u_{max}} = R_{max} \cdot \overset{\text{const.}}{f_{cu}} \cdot \underset{\text{const.}}{\gamma_c} \cdot \underset{\text{const.}}{b} \cdot \underset{\text{const.}}{d^2}$$

$$M_u > M_{u_{max}}$$



$$M_u = M_{u_{max}} + \Delta M$$

$$= R_{max} \cdot \frac{f_{cu}}{\gamma_c} \cdot b \cdot d^2 + \Delta M$$

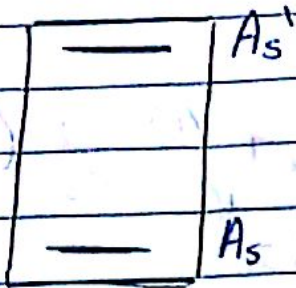


$$M_u = C_u \left(d - \frac{a}{2} \right) + C_s' (d - d')$$

$$= 0.67 \frac{F_{cu}}{\gamma_c} b a \left(d - \frac{a}{2} \right) + A_s' \frac{F_y}{\gamma_s} (d - d')$$

$$M_u = R_{max} \frac{F_{cu}}{\gamma_c} b d^2 + A_s' \frac{F_y}{\gamma_s} (d - d')$$

$$M_u = M_{u_{max}} + A_s' \frac{F_y}{\gamma_s} (d - d')$$



$$M_u = ??$$

$$\times \text{ Check } \mu = \frac{A_s}{b \cdot d} \times$$

$$\mu < \mu_{\max}$$

Safe

$\therefore A_s$ gibi no

$$\mu = \mu_{\max}$$

$$\frac{c}{d} = \frac{c_{\max}}{d}$$

$$A_{s_{\max}}$$

Safe

A_s gibi no

$$M_u = M_{u_{\max}}$$

$$\mu > \mu_{\max}$$

$$M_u = M_{u_{\max}} + \Delta M$$

A_s gibi no

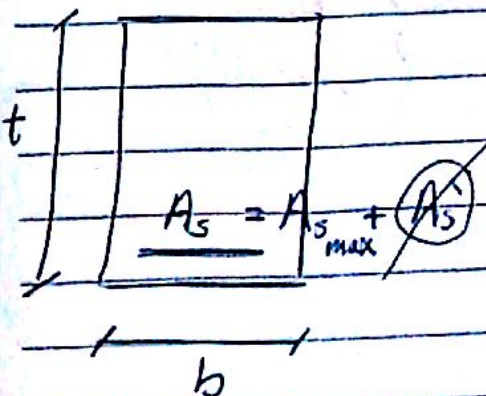
$$A_s = A_{s_{\max}} + A_s'$$

$$M_u = M_{u_{\max}} + A_s' \frac{f_y}{\gamma_s} (d - d')$$

Example: $b = \checkmark$ $t = \checkmark$ $A_s = \checkmark$ $M_u = ?$

$$\therefore M_u > M_{u_{\max}}$$

$$M_u = M_{u_{\max}} + \Delta M$$



$$A_s = A_{s_{\max}} + A_s'$$

$$\therefore A_{s_{\max}} = \mu_{\max} b d$$

$$\therefore \mu_{\max} = \frac{A_{s_{\max}}}{b d}$$

$$M_u = M_{u_{\max}} + \Delta M$$

$$= M_{u_{\max}} + A_s' \frac{f_y}{\gamma_s} (d - d')$$

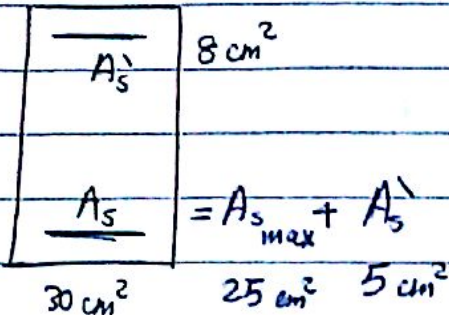
Zero

Date: _____

NO: _____

Ex: ②

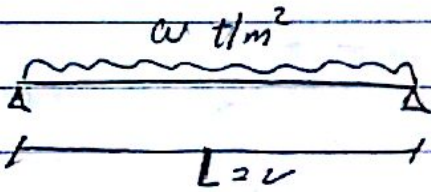
$$\mu = \frac{A_s}{b d} > \mu_{\max}$$



$$M_u = M_{u_{\max}} + A'_s \frac{f_y}{\gamma_s} (d - d')$$

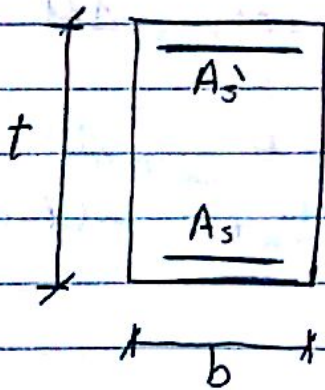
$$d - d' = 5 \text{ cm}$$

Ex: ③



$$M_u = \frac{w l^2}{8}$$

$$M_u > M_{u_{\max}}$$



$$\therefore M_u = M_{u_{\max}} + \Delta M$$

$$A_s = \checkmark$$

$$\therefore A_{s_{\max}} = \mu_{\max} b d = \checkmark$$

$$\therefore M_u = M_{u_{\max}} + A'_s \frac{f_y}{\gamma_s} (d - d')$$

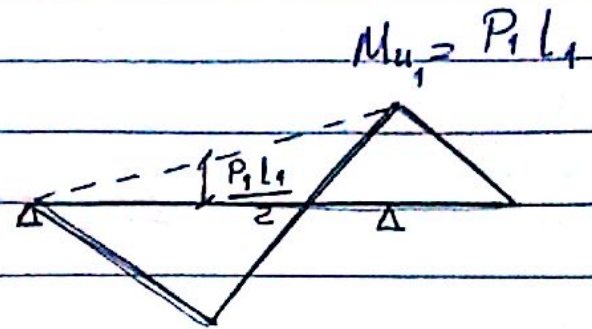
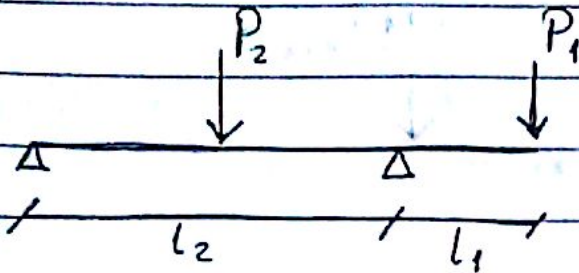
$$A'_s = A_s - A_{s_{\max}}$$

$$A'_s \text{ (مطلوب)}$$

Date:

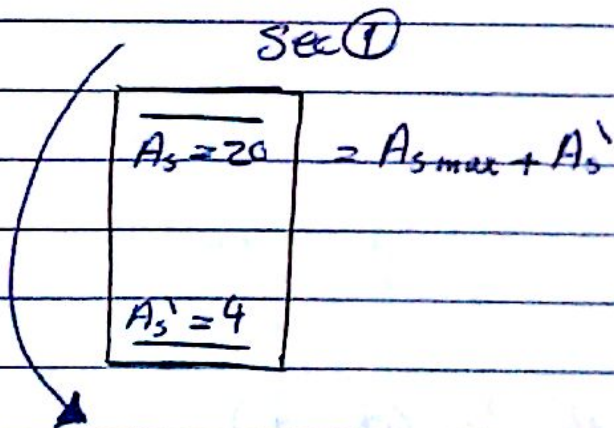
NO:

■ Ex:

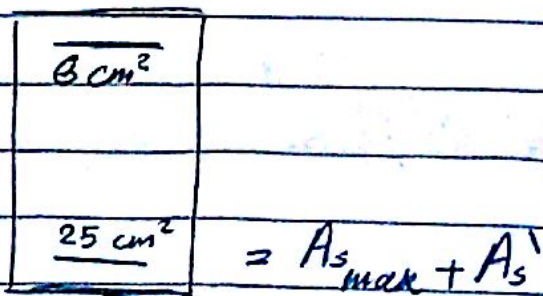


$$M_{u2} = \frac{P_2 l_2}{4} - \frac{P_1 l_1}{2}$$

$A_s' = 6$	$A_s = 20$
$A_s = 25$	$A_s' = 4$
sec ②	sec ①

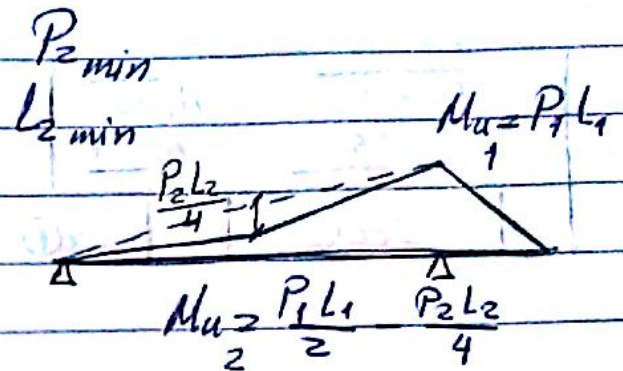
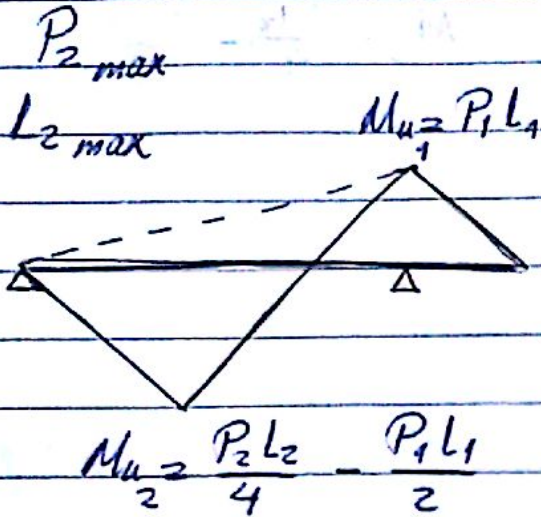
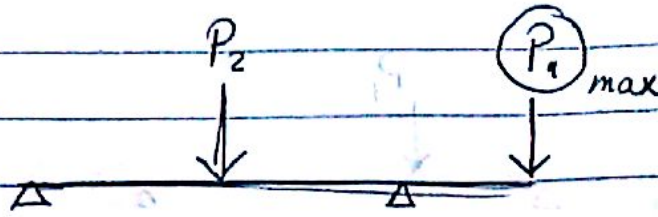


$$M_u = P_1 L_1 \Rightarrow P_1 \text{ max}$$



Date: _____

NO: _____



فحص في الفولاذ
check
for comp. steel

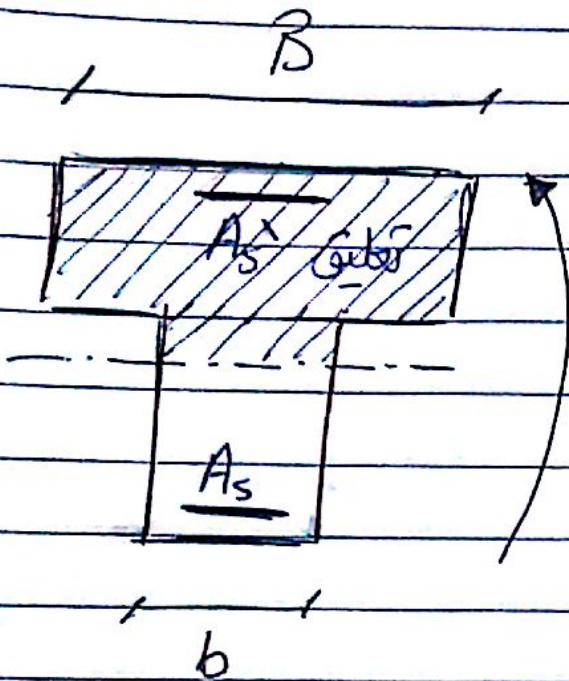
$$M_u = M_{u,max} + A_s' \frac{f_y}{\gamma_s} (d - d')$$

check: $\frac{A_s'}{A_s} > 0,4$

لو الفولاذ في حيز
Double R. في حيز الوصل

Date:

NO:

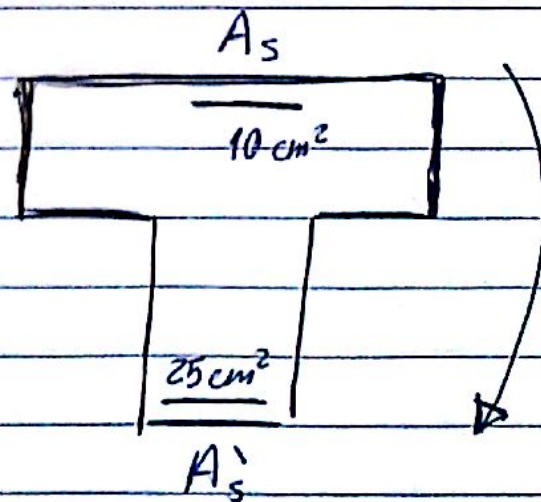
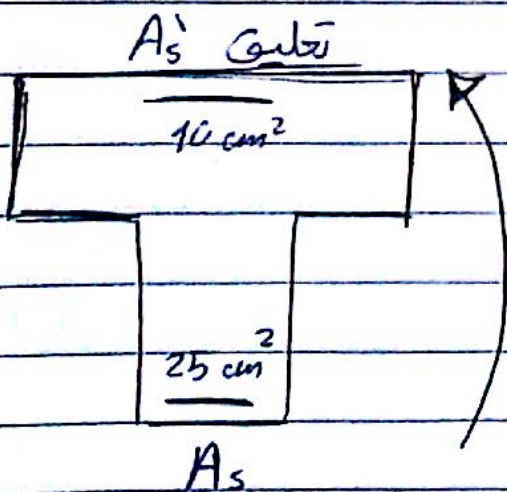


$$M_u = 0,67 \frac{f_{cu}}{\gamma_c} B a \left(d - \frac{a}{2} \right)$$

$$a = 1,93 \frac{A_s}{B} \frac{f_y}{f_{cu}}$$

$$a < t_s \Rightarrow \left(d - \frac{a}{2} \right)$$

$$a > t_s \Rightarrow \left(d - \frac{t_s}{2} \right)$$



~~XXXXXXXXXX~~